

Statistics Lecture 3



Feb 19-8:47 AM

class QZ 2 (open notes)

Consider the Sample below

1 2 2 2 8

1) $\sum x = 15$ ✓

2) $\sum x^2 = 77$ ✓

$n = 5$
 Mode = 2
 Range = $8 - 1 = 7$
 Midrange = $\frac{8+1}{2} = 4.5$
 Median = 2

3) $\bar{x} = \frac{\sum x}{n} = \frac{15}{5} = 3$ ✓

4) $S^2 = \frac{n \sum x^2 - (\sum x)^2}{n(n-1)} = \frac{5 \cdot 77 - 15^2}{5(5-1)}$

$S = \sqrt{S^2} = \sqrt{8} \approx 3$ $= \frac{160}{20} = 8$ ✓

Estimate $S \approx \frac{\text{Range}}{4} = \frac{7}{4} = 1.75 \approx 2$

Mar 6-10:57 AM

TI instructions:

- 1) To clear the Screen Clear
- 2) To quit 2nd MODE
- 3) To clear all lists 2nd + 4:ClearAll lists Enter
- 4) To reset all lists STAT Edit Enter
5:SetupEditor

Mar 13-8:14 AM

How to store data in a list

Store the Sample below in L1
List 1

12	15	10	18	11	
20	25	15	18	19	L1
					12 Enter
					↑ 15 "
					↑ 10 "
					⋮
					↑ 19 "

STAT Edit
1:Edit

Let's quit & clear the Screen

2nd MODE Clear

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To view a list:

2nd **1** **Enter**
L1

{ 12 15 10 18 . . . 19 }

→ → →
 ← ← ←

How to Sort a list:

STAT **Edit** **2nd** **1** **Enter**
2:SortA L1

Let's view L1, and make Stem Plot

2nd **1** **Enter**
L1

{ 10 11 12 15 . . . 25 }

→ → →
 ← ← ←

1|01255889
 2|05

Mar 13-8:26 AM

How to find \bar{x} & S :

STAT **→** **CALC** **1:1-VarStats** **2nd** **1**
 with menu No Menu
 List: L1 L1 **Enter**
 Freq List: **clear**
Calculate $\bar{x}=16.3$
 $S=Sx=4.620$

Min = 10
 Q1 = 12
 Med. = 16.5
 Q3 = 19
 Max = 25

5-Number Summary

$n=10$

what about S^2 ?

VARS
5: Statistics
3: Sx
 x^2 **Enter**
 $S^2=21.34$

To convert to a reduced fraction

Math **1: Frac** **Enter**

$S^2 = \frac{1921}{90}$

Mar 13-8:34 AM

Find \bar{x} & S .

STAT \rightarrow **CALC** \rightarrow **1: 1-Var Stats** \rightarrow **2nd** **1**

$\bar{x} = 29.7$
 $S = S_x = 10.423$
 $n = 20$

With Menu
 List: L1
 FreqList: **clear**
Calculate

NO Menu
 L1
Enter

Find S^2 in reduced fraction.

Vars **5: Statistics** **3: Sx**
Math **1: Frac** **Enter**
 $S^2 = \frac{10321}{95}$
Math **2: Dec** **Enter**
 $S^2 = 108.642 \dots$

Clear all lists **2nd** **+** **4: clear all list** **Enter**
 clear the screen **clear**

Min = 15
 Q1 = 20
 Med = 28.5
 Q3 = 37.5
 Max = 50

Mar 13-8:57 AM

Working with Grouped data:

class limits	class F	class MP
14 - 20	4	17
21 - 27	8	24
28 - 34	10	31
35 - 41	3	38

Find \bar{x} & S .

class MP \rightarrow L1
 class F \rightarrow L2

L1	L2
17	4
24	8
31	10
38	3

STAT \rightarrow **CALC** \rightarrow **1: 1-Var Stats** \rightarrow **2nd** **1**

With Menu
 List: L1
 FreqList: L2
Calculate

NO Menu
 L1, L2
Enter
quit **end** **Mode**

$\bar{x} = 27.36$
 $S = S_x = 6.428$
 $n = 25$

Find S^2 in reduced fraction

Vars **5: Statistics** **3: Sx** **Math** **1: Frac** **Enter**
 $S^2 = \frac{12397}{300}$

Mar 13-9:20 AM

Complete the chart below ✓ CW = 10
n = 30

class limits	class BNDRS	class MP	class F	Cum. F	Rel. F	% F
50 - 59	49.5 - 59.5	54.5	8	8	.267	26.7%
60 - 69	59.5 - 69.5	64.5	12	20	.400	40.0%
70 - 79	69.5 - 79.5	74.5	10	30	.333	33.3%

Rel. F = $\frac{F}{n} = \frac{F}{30}$

Find \bar{x} , S, and S^2 of this grouped data.

clear all my lists 2nd + 4:clear all lists

class MP → L1 L1 L2 Enter

class F → L2

54.5	8	$\bar{x} = 65.1\bar{6}$ $S = S_x = 7.849$ $n = 30$
64.5	12	
74.5	10	

STAT → CALC

1:1-Var Stats

List: L1 NO MENU

FreqList: L2 L1, L2 Enter

Calculate 7

$S^2 = \frac{5360}{87}$

Mar 13-9:34 AM

I randomly selected 28 exams. Here are the Scores

75	83	90	65	Store in L1 ✓ Sort L1 ✓ View L1 ✓ Make Stem Plot
55	100	70	80	
95	98	58	60	
68	50	72	83	
93	100	99	90	
72	85	89	74	
69	73	88	88	

5	0 5 8
6	0 5 8 9
7	0 2 2 3 4 5
8	0 3 3 5 8 8 9
9	0 0 3 5 8 9
10	0 0

Mar 13-9:50 AM

$\begin{array}{r l} 5 & 058 \\ 6 & 0589 \\ 7 & 022345 \\ 8 & 0335889 \\ 9 & 003589 \\ 10 & 00 \end{array}$	<p>1) P_{30}</p> $L = \frac{30}{100} \cdot 28 = 8.4$ $L = 9 \quad P_{30} = 9\text{th element} = \boxed{72}$ <p>2nd 1 (9 Enter</p>
<p>2) Median P_{50}</p> $L = \frac{50}{100} \cdot 28 = 14$ $P_{50} = \frac{14\text{th} + 15\text{th}}{2} = \frac{80 + 83}{2}$	<p>2nd Enter change 9 to 14 enter =81.5</p> <p style="text-align: center;">$14 \neq 15$</p>

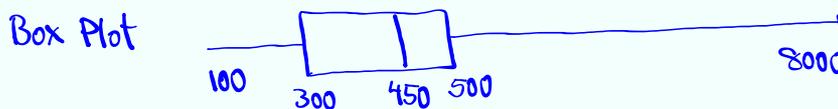
Mar 13-9:59 AM

$\begin{array}{r l} 5 & 058 \\ 6 & 0589 \\ 7 & 022345 \\ 8 & 0335889 \\ 9 & 003589 \\ 10 & 00 \end{array}$	<p>Find the percentile ranking of 65. \rightarrow Find k such $\#$ Below that $P_k = 65$</p> $k = \frac{B}{n} \cdot 100, \text{ Round to whole \%}$ $k = \frac{4}{28} \cdot 100 = 14.285 \dots \approx 14$ <p style="text-align: center;"> $\frac{14\% \quad 86\%}{P_{14} = 65} \quad P_{14} = 65$ </p>
<p>Find k such that $P_k = 88$.</p> $k = \frac{B}{n} \cdot 100 = \frac{17}{28} \cdot 100 = 60.714 \approx 61$	<p>$P_{61} = 88$</p> <p style="text-align: center;"> $\frac{61\% \quad 39\%}{P_{61} = 88}$ </p>

Mar 13-10:04 AM

Consider the following 5-number summary

100 300 450 500 8000



$$IQR = Q_3 - Q_1 = 500 - 300 = 200$$

$$\text{Upper Fence} = Q_3 + 1.5(IQR) = 500 + 1.5(200) = 800$$

$$\text{Lower Fence} = Q_1 - 1.5(IQR) = 300 - 1.5(200) = 0$$

Possible outliers Range

$$800 - 8000$$

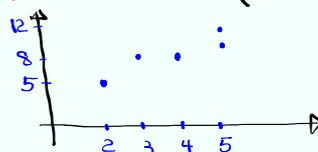
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Working with ordered-Pairs
(x, y)

x	y
2	5
3	8
4	8
5	12
5	10

1) $n = 5$

2) Plot these Points (Scatter Plot)



Clear all lists

$x \rightarrow L1$, $y \rightarrow L2$

STAT \rightarrow **CALC**

2: 2-Var Stats

with Menu

xlist: L1

ylist: L2

freq list: **clear**

calculate

No Menu

L1, L2 **enter**

1

$$\sum x = 19$$

$$\sum x^2 = 79$$

$$n = 5$$

$$\sum y = 43$$

$$\sum y^2 = 397$$

$$\sum xy = 176$$

Mar 13-10:31 AM

STAT → **CALC**
 8: LinReg(a+bx)

with Menu
 x list: L1
 y list: L2
clear
Calculate

NO Menu
 L1 , L2 **enter**
7

a = 1.559
b = 1.853
r² = .858
r = .926

IF r & r² missing:
end 0
 ↓ ↓ ↓ ... ↓
Diagnostic On
Enter Enter

Mar 13-10:40 AM

I randomly Selected 5 students.

Study time	QZ Score
2	7
3	8
4	10
4	8
5	10

Scatter Plot

Study time → x → L1
 QZ Score → y → L2

STAT → **CALC**
 8: LinReg(a+bx)

a = 5
b = 1
r² = .722
r = .850

Mar 13-10:46 AM

Class QZ 3 (open notes)

use the Sample below **find**

28	32	20	18
25	19	30	45
35	26	18	35
48	50	36	38

$$1) \bar{x} = 31.4375 \approx \boxed{31}$$

$$2) S = S_x = 10.405 \approx \boxed{10}$$

$$3) S^2 = \frac{8661}{80}$$

} Round to
whole

} Reduced
fraction

Mar 13-10:54 AM